

Apocalyptic quantum gravity



David Wakeham
UBC Gravity Seminar
April 28, 2021

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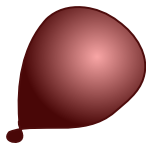
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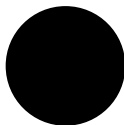
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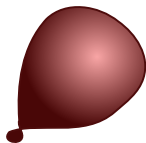
hard



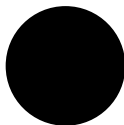
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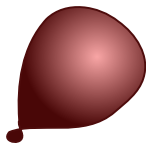


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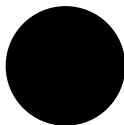
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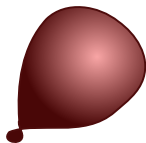


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- ▶ The “**easy**” **problem** is black holes because we can plonk them in a different-looking spacetime, **AdS/CFT**.

AdS/CFT in a nutshell

AdS/CFT in a nutshell

- ▶ Let's consider quantum gravity

AdS/CFT in a nutshell

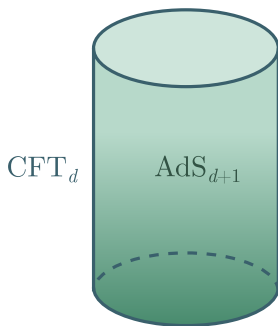
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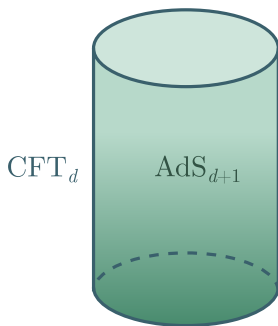
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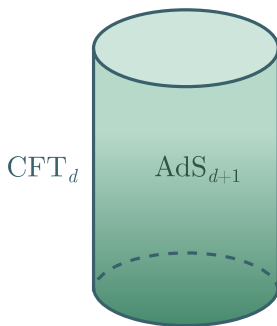
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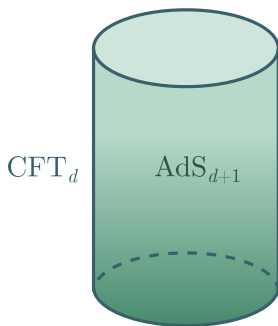
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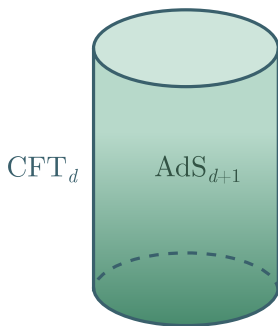
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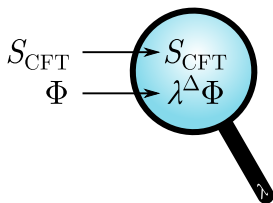
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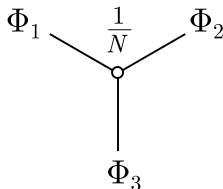
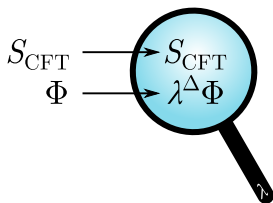
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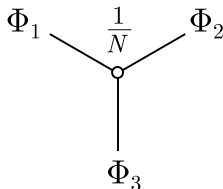
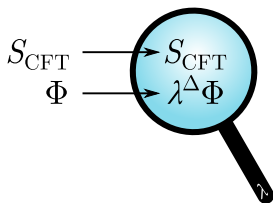
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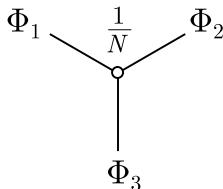
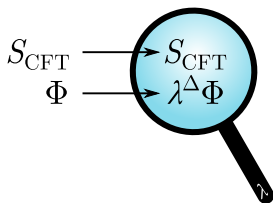
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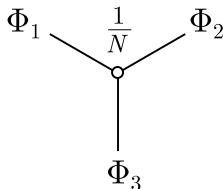
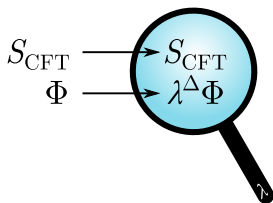
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States and metrics

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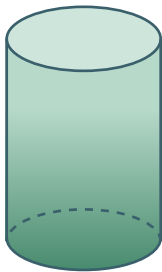
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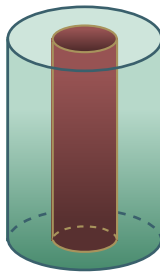
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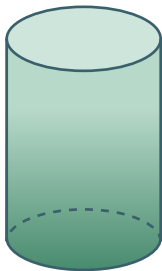
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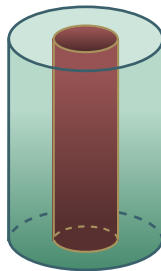
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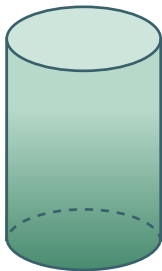


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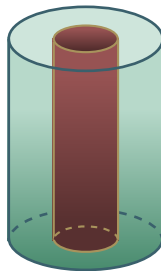
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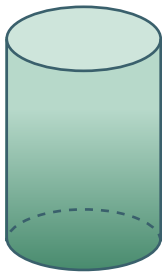


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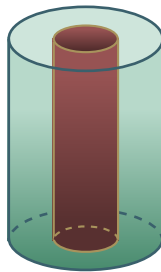
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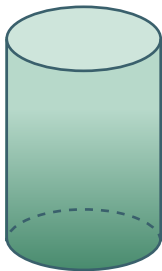


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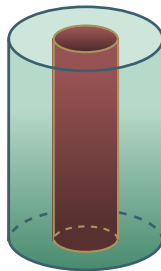
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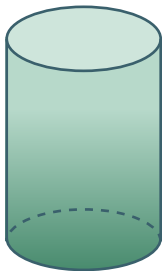


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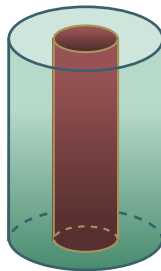
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- ▶ More interesting: **canonical thermal state**, where the probability of observing $|E\rangle$ is proportional to $e^{-\beta E}$.
- ▶ This turns out to be dual to an AdS **black hole**!³

Eternal/external

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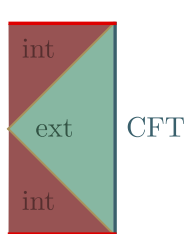
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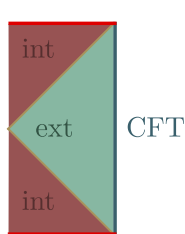
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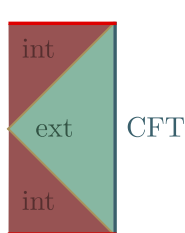


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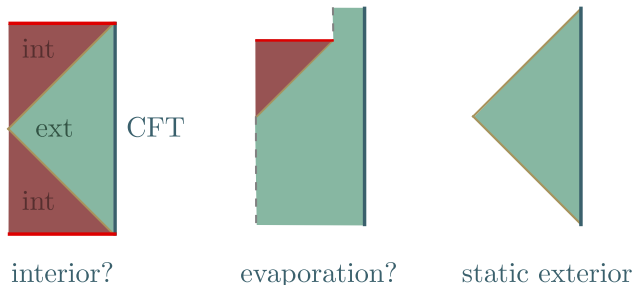


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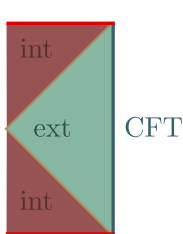
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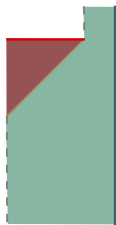
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interior?



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static exterior

- ▶ Problem: **we can't do either!** It's just the **static exterior geometry**, so no interior or evaporation.

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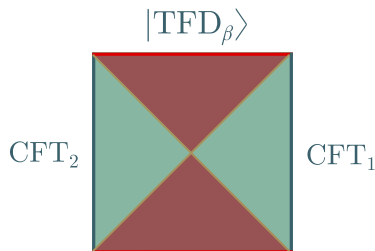
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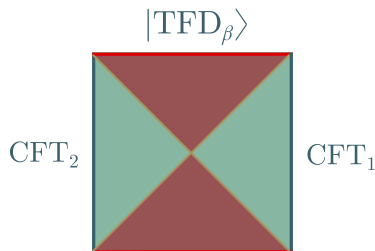
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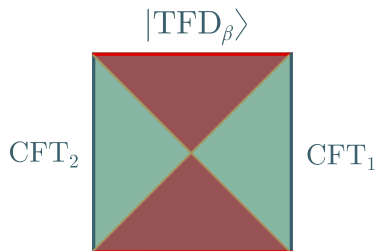


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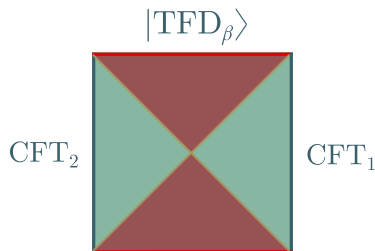


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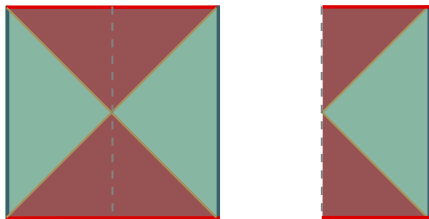
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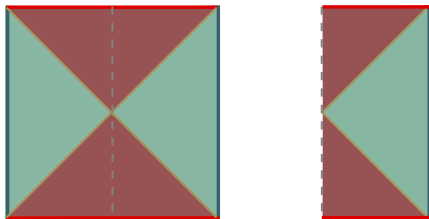
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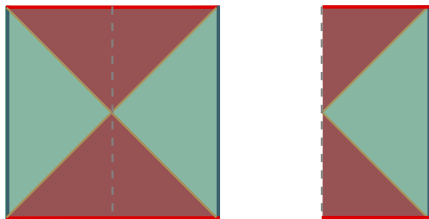
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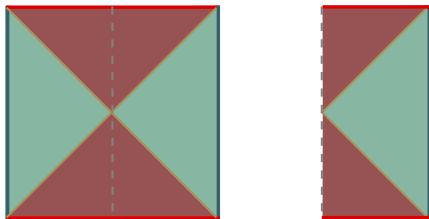
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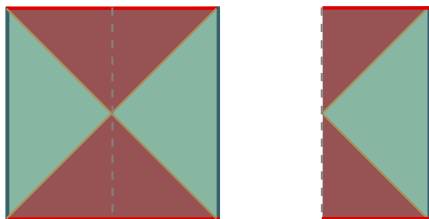
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Wick's trick

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Wick's trick

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Wick's trick

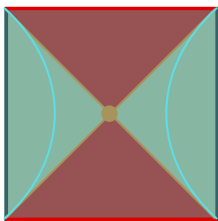
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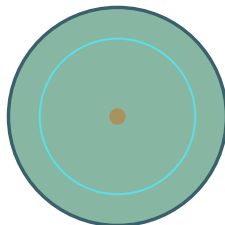
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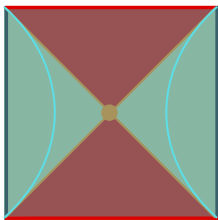
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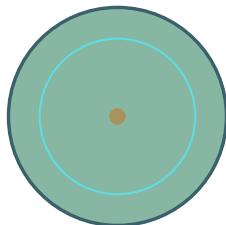
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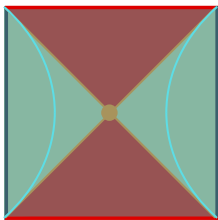


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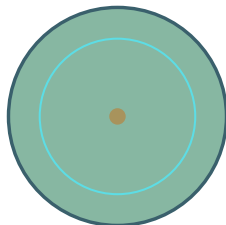
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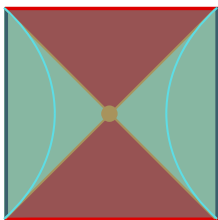


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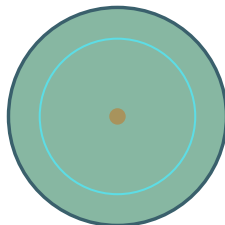
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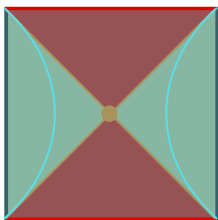


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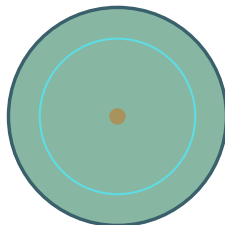
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Boundary states

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Boundary states

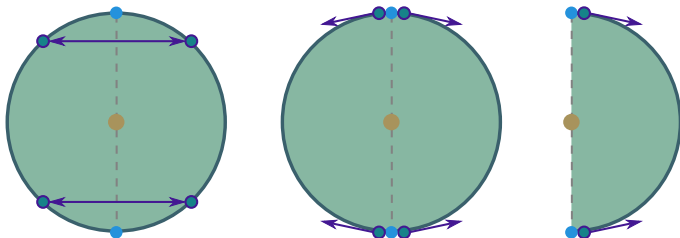
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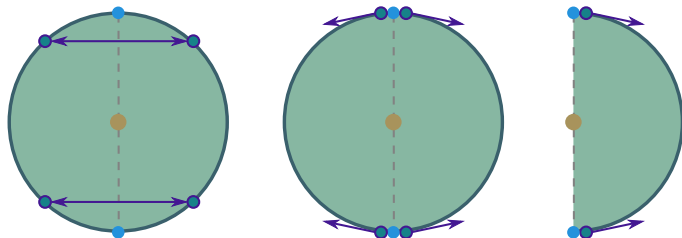
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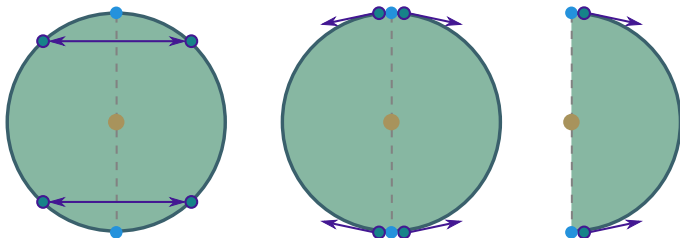
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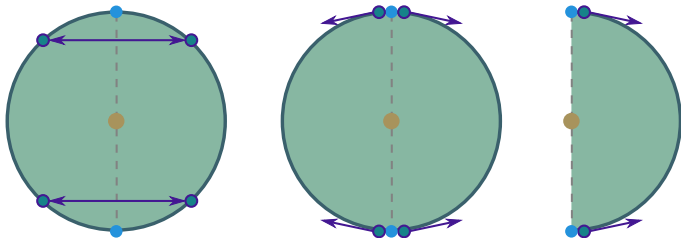
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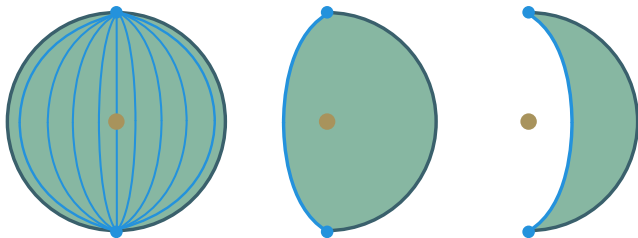
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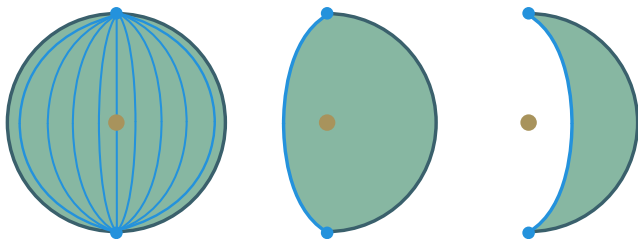
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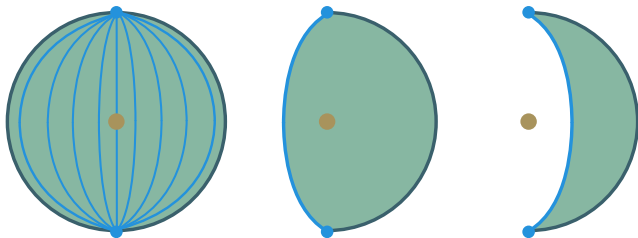
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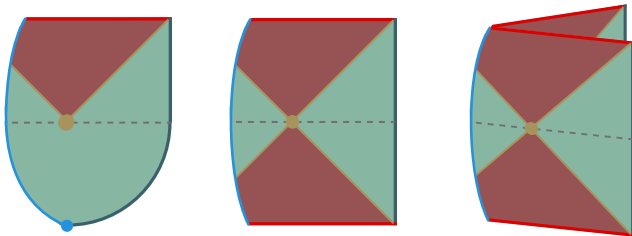
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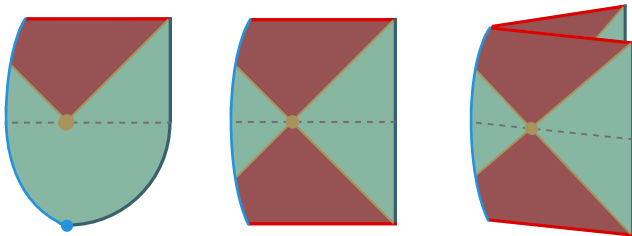
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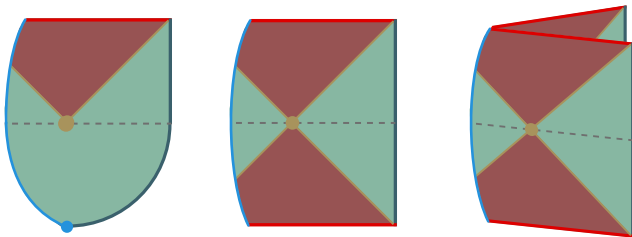
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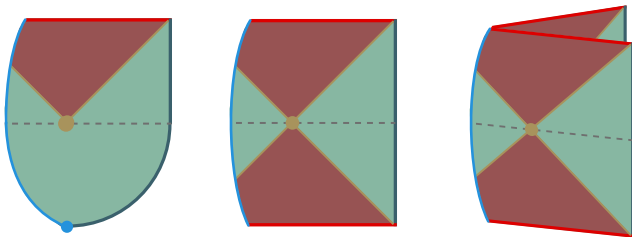
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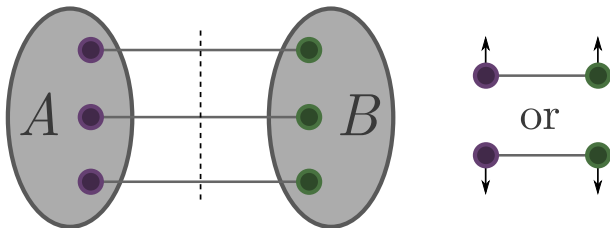
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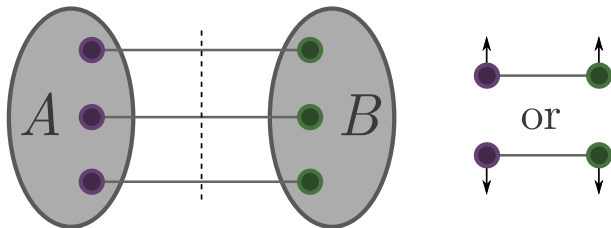
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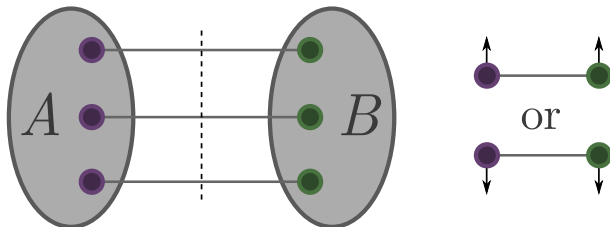
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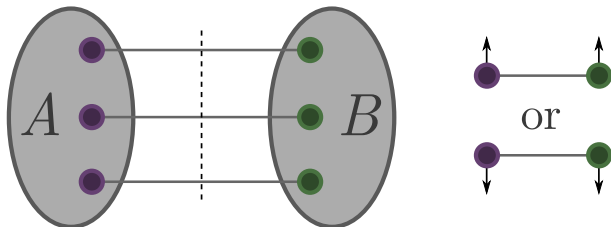
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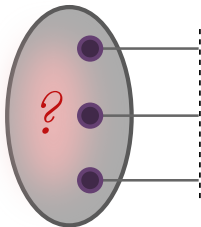
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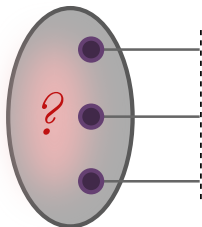
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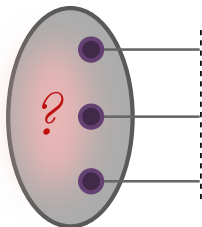


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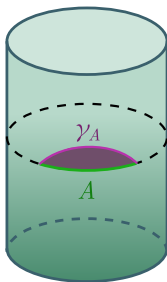
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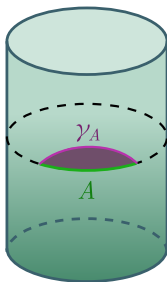
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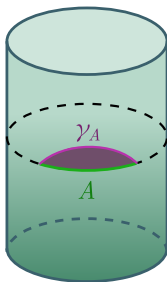


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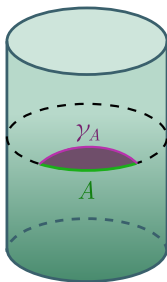


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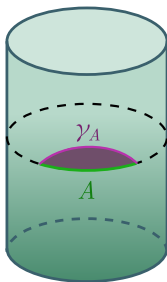


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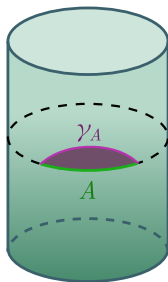


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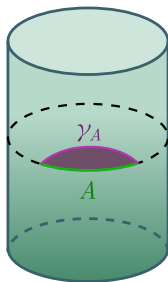


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Apocalyptic RT

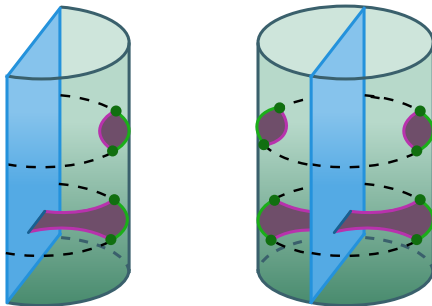
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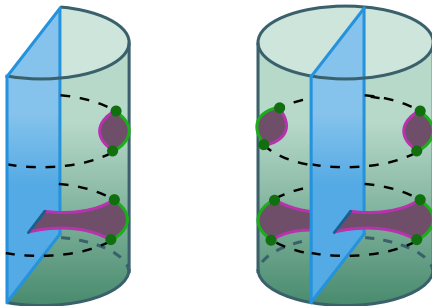
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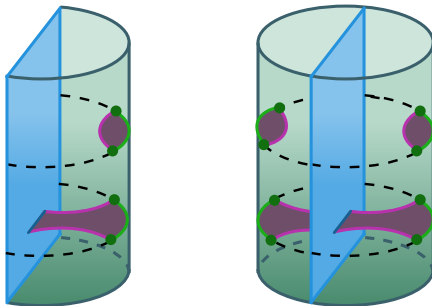
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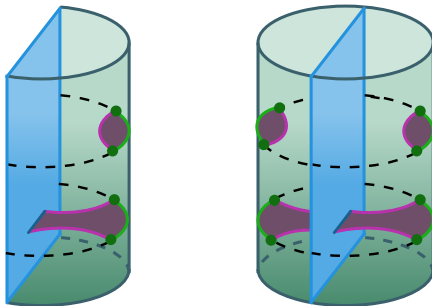
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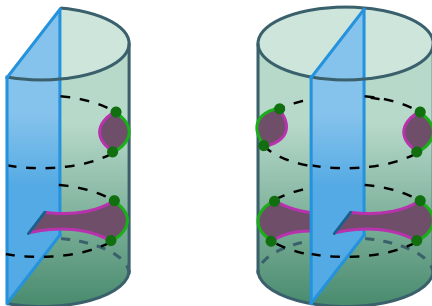
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- ▶ (It's the **method of images** for quantum gravity.)

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Peeking behind horizons

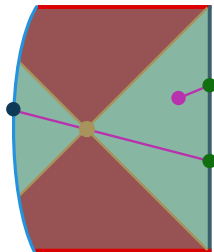
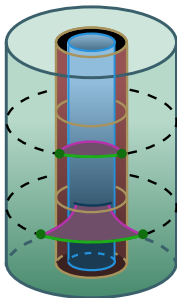
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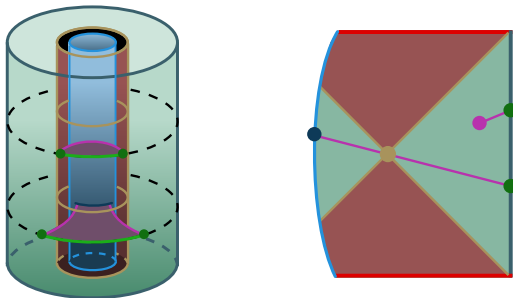
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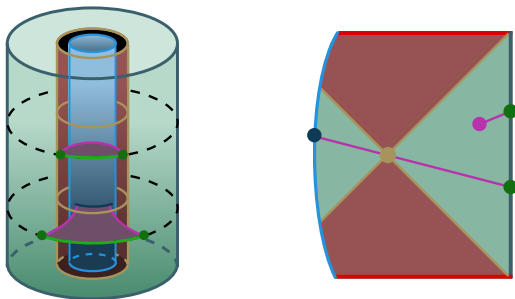
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- ▶ We did explicit calculations⁹ to find **regimes γ_A falls in**.

Peeking behind horizons

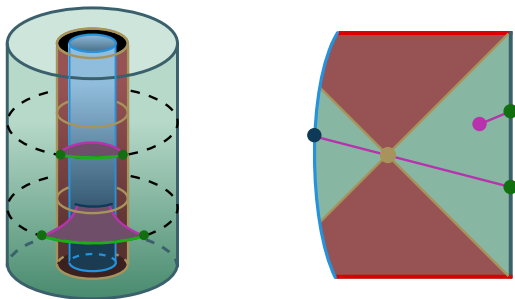
- ▶ Let's use our apocalyptic RT formula **in the black hole**.
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Under the microscope

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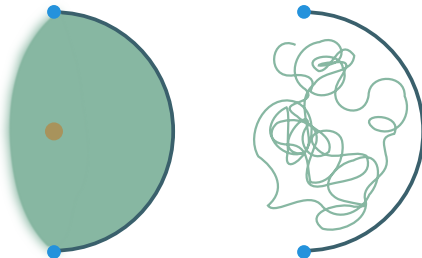
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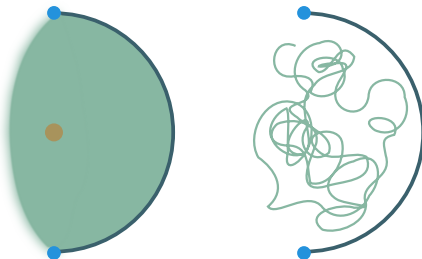
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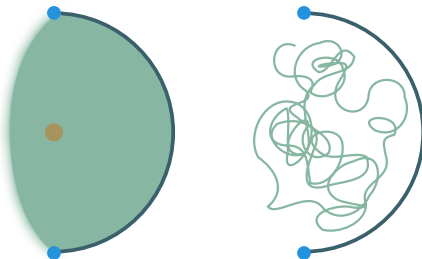
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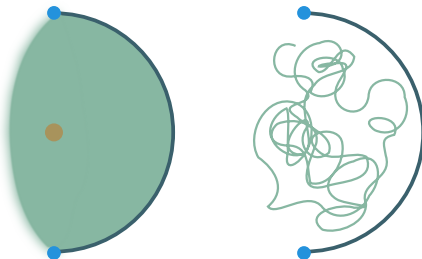
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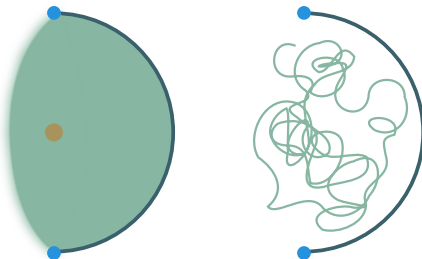
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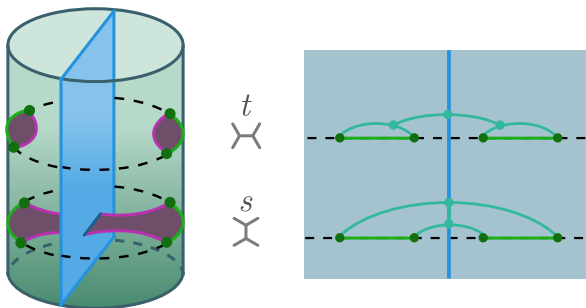
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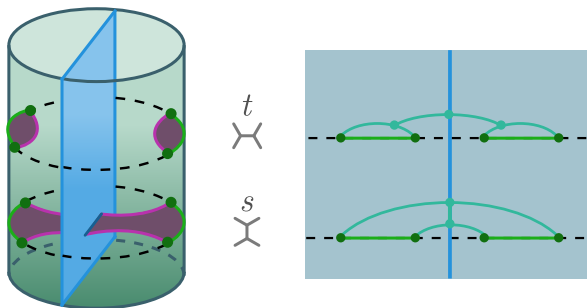
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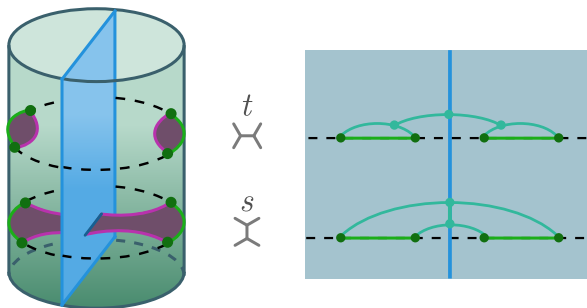
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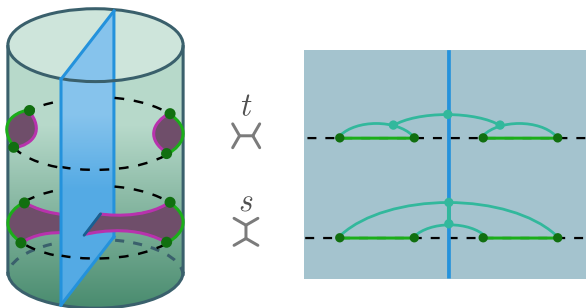
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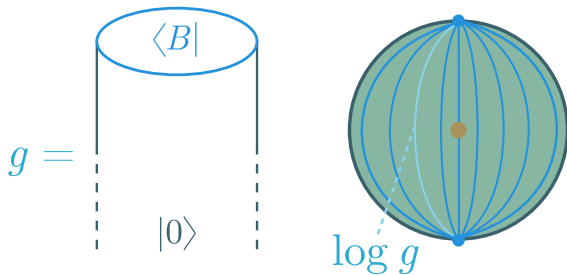
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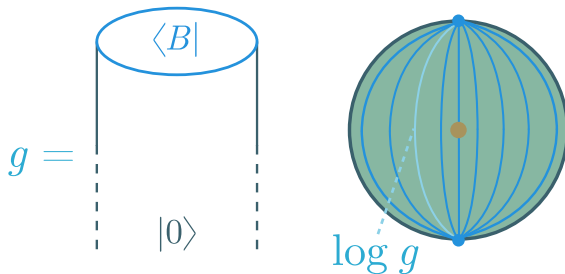
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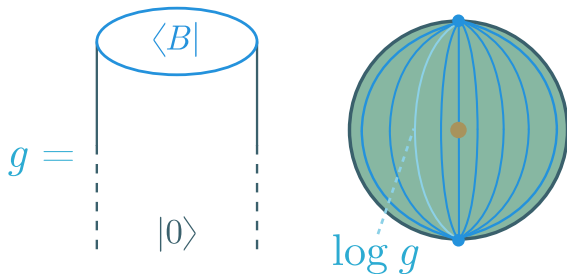
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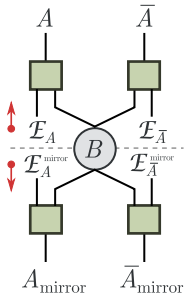
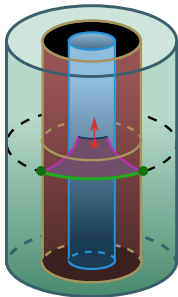
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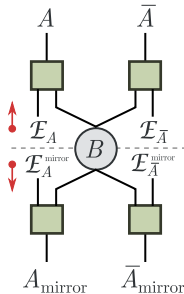
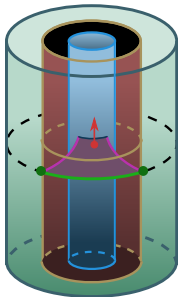
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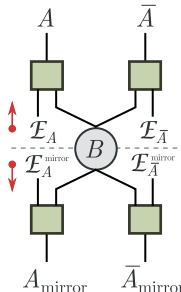
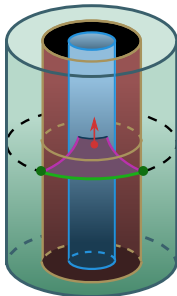
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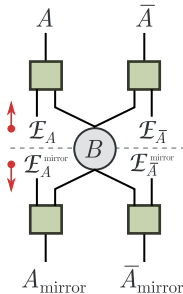
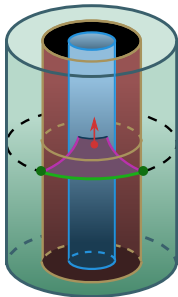
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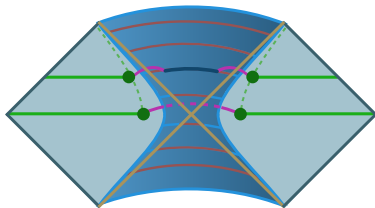
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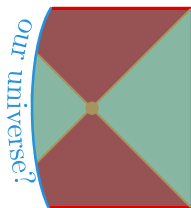
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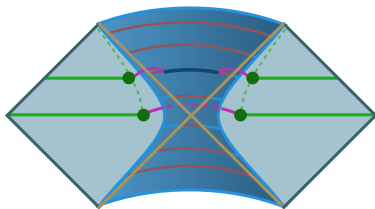
information paradox!



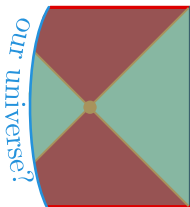
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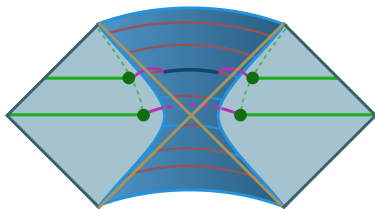


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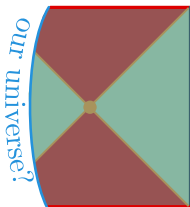
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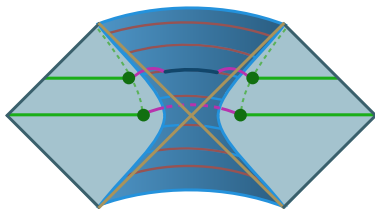


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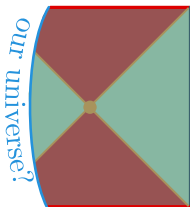
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- ▶ Circling back round to our initial motivation, the brane itself looks like a **Big Bang/Big Crunch cosmology**.
- ▶ The trick is to **localize gravity to the brane**.¹⁴

Conclusion

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Thanks for listening!

References

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